REO: A generic RAID Engine and Optimizer

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Abstract

Present day applications that require reliable data storage use one of five commonly available RAID levels to protect against data loss due to media or disk failures. With a marked rise in the quantity of stored data and no commensurate improvement in disk reliability, a greater variety is becoming necessary to contain costs. Adding new RAID codes to an implementation becomes cost prohibitive since they require significant development, testing and tuning efforts. We suggest a novel solution to this problem: a generic RAID Engine and Optimizer (REO). It is generic in that it works for any XOR-based erasure (RAID) code and under any combination of sector or disk failures. REO can systematically deduce a least cost reconstruction strategy for a read to lost pages or for an update strategy for a flush of dirty pages. Using trace driven simulations we show that REO can automatically tune I/O performance to be competitive with existing RAID implementations.

1 Introduction

Until recently, protecting customer data from loss due to media failure and/or device failures meant storing it using one of five RAID levels [32]. To handle higher performance and reliability needs of customers, storage vendors have deployed hierarchical codes like RAID 51. These codes are offered as a result of juggling the inherent risk-reward trade-off from a software engineering standpoint and not out of any merits, whether in storage efficiency or performance. Since these codes can be composed by re-using e.g., hierarchically, the basic RAID set, source code added was minimal. This meant that product marketing needs could be satisfied with low test expense.

There were good reasons why only a few RAID codes were supported in traditional RAID controller implementations (firmware). Firmware complexity grows with every supported RAID code, increasing development and test costs. When firmware becomes a large collection of specific cases it becomes hard to do path length optimizations. From a software maintainability standpoint, a collection of *if... then... else...* code blocks makes firmware readability harder and more prone to bugs. Each roll out of a RAID code potentially requires field upgrades.

Since deploying firmware changes is painful there is a general mindset to avoid it at all costs. However, recent trends in storage technology and customer focus are forcing a re-evaluation. First, no single RAID code satisfies all aspects of data storage. Supporting a variety of RAID codes becomes valuable for effective information lifecyle management where data should be stored at performance, reliability and efficiency levels that are proportionate to its business value. Second, the nature of reference data is that while the dataset grows from gigabytes to petabytes its reliability must remain relatively constant. Using the same RAID code for all sizes is not practical since disk failures grow with capacity[8, 36]. A third reason is the growing popularity of modular systems where bricks [17] are the building blocks to systems that scale in capacity and performance [36, 31, 2, 37]. Some of these systems [11] even simplify management using fail-in-place strategies. Another trend is to use low cost serial ATA (SATA) disks in building large systems [26]. SATA disks have hard error rates that are 10x higher than comparable SCSI disks [10, 18] while being 30-50% cheaper. Providing high data reliability using less reliable disks requires a greater variety of RAID codes.

In light of the tension to provide a variety of RAID codes without compromising the quality, performance, and maintainability of the firmware, we can draw up a list of requirements for an ideal solution: (1) It should allow for adding new RAID codes without firmware complexity, (2) It should easily support popular RAID codes e.g., XOR-based ones which can be implemented efficiently in hardware and/or software, (3) It should automatically handles any RAID code related error handling e.g., read error to a failed sector or disk, (4) Since error handling constitutes a large fraction of any RAID implementation, ideally, the solution should fold fault-free and fault-ridden cases into common code paths. (4) It should simplify nested error paths e.g., in the process of reconstructing a lost block due to a previous failure, a new sector or disk failure is discovered. While the successful completion can occur only if the RAID code permits, an ideal solution must figure out automatically how to do reconstructions. (5) It should automatically tune I/O performance by leveraging dynamic state e.g., cached pages. (6) It should offer informal arguments for correctness, if not formally provable.

Our contributions

We present our efforts at building a generic RAID Engine and Optimizer (REO) fits the above requirements. It is generic in that it works for any XOR-based erasure (RAID) codes (including N-way mirroring) and under any combination of sector or disk failures. In a typical deployment REO routines are invoked by the block data cache in the I/O stack to read, write, scrub, rebuild, or migrate data stored on disks using RAID codes. REO can systematically deduce reconstruction and update strategies and execute them. In addition, an online optimizer within REO can select a least cost strategy for every read or write based on the current cache content. This optimizer can be configured to minimize any system level objective e.g., disk I/O or memory bus usage. By parameterizing fault state, REO can eliminate myriads of cases including those involving nested recovery into a single code path. Finally, by building on results that have been formally proved, we can informally argue about the correctness of REO.

This paper is structured into a high level overview of REO (Section 3) followed by detailed description (Sections 4- 6). While these sections focus on read and write operations, Section 7 discusses scrub, rebuild, and migrate. An evaluation of the efficacy of optimization is discussed in Section 8. Some adaptations to future trends in I/O architecture are presented in Section 9.

2 Related work

There has been no dearth of RAID codes proposed until now e.g., EVENODD[3], generalized EVENODD [4], X-code [42], RDP [12], WEAVER [19]. Recently, there have been a few non-XOR code implementations [8, 33] but these have remained niches since they offer no special advantage over the simplicity of XOR based codes.

One past effort that has focused on providing firmware environments that permit rapid prototyping and evaluation of redundant disk array architectures was RAIDframe[14]. It modularized the basic functions that differentiate RAID architectures — mapping, encoding and caching. Such a decomposition allowed each aspect to be modified independently creating new designs. Array operations were modeled as directed acyclic graphs (DAGs), which specified the architectural dependencies (and execution) between primitives. While it allowed a structure to specify exception handling, RAIDframe lacked any ability to automatically tune performance.

Recently, RAID system-on-chip (SOC) products [27], [6] and [25] have become available. The Aristos SOC, which exemplifies this category, contains an embedded processor, DMA/XOR engines and host and disk interface logic. Since the processor is programmable it is conceivable that they could support a variety of RAID codes. However, the problem with it is that all error paths must be specified as callbacks (much like RAIDframe) which must be written by the developer. Further, it is unclear to us how automated (if at all) the performance tuning is.

3 Overview

REO is a set of routines invoked by a (block or file) data cache when reading or writing data to a RAID coded volume e.g., RAID 1, RAID 5, EVENODD, etc., as shown in Figure 1. In it, applications generate read and write requests to the I/O subsystem that are serviced by a data cache. With write-back caching, application writes are copied to pages in the data cache and marked dirty. At a later time, as determined by the page replacement policy, dirty pages are flushed (written out) to disks. With read caching, when possible, application reads are served out of the data cache. On a read miss, the cache first fetches the data from the disk(s) and then, returns it to the application. Most data caches dynamically partition writeback and read pages to handle a variety of application workloads. In many RAID controllers and filers [23] the write-back cache is protected from unexpected power failure.



Figure 1: Figure shows a typical deployment of REO within the I/O stack. One or more applications generate read or write calls to RAID coded volumes. These requests are first attempted to be served by the block data cache. If a read miss occurs or a page needs to be flushed then, REO routines are invoked. REO routines include RAID housekeeping functions like rebuild, migrate and scrub. These routines can support any RAID code, under any set of sector or disk failures while simultaneously considering the current cache state.

3.1 Use cases for REO

REO routines are invoked by the data cache in four scenarios:

- 1. Read on a miss (reo_read): The virtualized block address of the requested page(s) is translated to its physical block address within the identified disk. In the fault-free case, disk read(s) is issued. If that disk (or particular sectors within it) has failed then, a reconstruction must be done by REO by reading related blocks according to the RAID code. Sometimes, reconstruction is impossible in which case a read error is returned.
- 2. Flush a dirty page (reo_write): When the cache replacement policy has picked a victim (dirty) page to be written to the disk, the virtual block address of the victim is translated to its physical block address within the identified disk. REO must identify the dependent parity block(s) from the RAID code information and figure out how to update them. This use case covers write-through writes e.g., when write-back caching is disabled.
- 3. Rebuild a lost page (reo_rebuild): Generated by an internal housekeeping routine to repair lost data (due to sector or disk failure), REO must first reconstruct the lost page using the redundant information within the RAID code and then, write it to a new location. Rebuild can be viewed as a composite operation – reconstruct read followed by write.
- 4. Migrate a page (reo_migrate): Triggered by an administrative action, migration is invoked to change the RAID code of a set of pages. Migration includes varying the span (rank) of disks (8disk RAID 5 to 5-disk RAID 5) and changing the RAID code (RAID 5 to EVENODD). Like rebuild, migration can be viewed as a composition – read, using the old code, followed by write, using the new code.

Since rebuild and migrate are compositions, we focus primarily on describing reo_read and reo_write operations. We defer discussing reo_rebuild and reo_migrate to Section 7.

3.2 Two components of REO

REO routines can be functionally partitioned into two components: a RAID Engine which figures out *what* is to be done, and an Execution Engine which figures out *how* it gets done. Figure 2 sketches this breakdown. The RAID engine transforms the input arguments into an I/O plan which comprises a set of blocks to be read, a set to be XOR-ed, and a set to be written. Such an I/O plan is input to the execution engine which issues the necessary disk reads and writes and XOR operations.

In addition to the basic operation type (reo_read or



Figure 2: Figure shows a component breakdown of REO into a RAID Engine and Execution Engine. The RAID Engine takes inputs to compute an I/O plan. All its inputs are readily available within the meta-data, system data structures and/or cache directory. An I/O plan includes a set of pages that must be read from the disks, a set of pages that must be XOR-ed, and a set of pages that must be written. Depending on the inputs some of these sets may be empty. The Execution Engine detects and handles error handling during the execution of an I/O plan. If it encounters any errors then, it aborts the I/O plan, modifies the fault configuration vector, and resubmits the operation to the RAID Engine. An online Optimizer within the RAID Engine selects strategies that suit a configured system level objective.

reo_write) and their arguments — the page(s) block address, starting virtual block address, and number of bytes to be read or written — the RAID Engine requires the following inputs to generate the I/O plan:

- A concise description of the RAID code, available from the meta-data.
- A description of the physical arrangement of blocks in the RAID code called the layout, available from the meta-data.
- A description of known sector or disk failures called the fault configuration, available from system managed data structures.
- A list of clean and dirty pages presently in the data cache surronding the page(s) to be read or written, available from the data cache directory.

A final input to the RAID Engine is a resource optimization objective. This can include (but not limited to) criteria like minimizing disk I/O or minimizing memory bus bandwidth. This input guides the Optimizer, a component within the RAID Engine, whenever it has a choice of strategies for any read or write.



Figure 3: Figure illustrating two (of a total of eight) strategies possible while flushing a set of dirty pages for a 5-disk left-symmetric RAID 5 coded volume. On the left, the shaded pages show the dirty pages that are within a single stripe neighborhood of a victim page marked"X". On the right, we show the resulting pages that would have to be read and written if one strategy were chosen over the other.

The Optimizer has little variety for fault-free reads where the only reasonable option is to read the required page directly from the appropriate disk. For writes there can be more choices. Each choice can require a different number of disk reads and/or XOR operations. In such cases, the configured objective function is used by the optimizer to guide selection.

Before starting on an I/O plan, the Execution Engine acquires all necessary page and stripe locks. Then, it carries out the plan in three phases: first, it submits the disk reads (if any); next, it performs the XOR operations (if any); finally, it submits the disk writes (if any). During any of these steps, if it encounters failed sectors or disks, it re-submits the entire operation to the RAID Engine along with the newly discovered fault state. In Figure 2 shows this resubmission step. One advantage of such a structure is that the recovery code is no different from the main code path.

3.3 Supporting mirrors

One popular RAID code that, at a first glance, appears not to be XOR-based is RAID 1 and, more generally, Nway mirroring. However, such codes are technically degenerate cases of XOR-based erasure codes where each additional copy can be thought of as parity computed from the primary copy and implicit zero entries for a comparable erasure code (RAID 1 with RAID 5, 3-way mirror with EVENODD). Our RAID Engine leverages this to include support for mirrors and striped mirror codes like RAID 10. Without loss of generality, we assume that RAID codes have parity elements in the rest of the paper.

3.4 A RAID 5 example

Before describing the construction of reo_read and reo_write, we work through an example write that illustrates the choices available and how different I/O

plans entail different costs in terms of disk reads and writes and the number of XORs. Figure 3 illustrates this example for a left-symmetric RAID 5 code. In the left figure, say that the dirty pages within a one stripe neighbourhood of the victim page (marked "X") are shaded grey and flushed in a single operation. There are wo strategies possible to perform this operation (shown on right). Each strategy is illustrated by two sets of shaded pages — read pages on left and dirty pages on right. Assuming that a RAID controller can coalesce requests to contiguous blocks on a disk, the approach on the top labelled "Strategy A" requires 4 reads, 6 writes, and 14 pages of memory bus usage for XOR, while "Strategy B" requires 3 reads, 6 writes, and the transfer of 15 pages on the memory bus.

Depending on the configured system level objective REO will choose between these two strategies. Strategy A would be appropriate if memory bus usage were to be minimized; Strategy B is better for disk I/O. The two strategies shown in Figure 3 are from a possible eight.

4 RAID engine

In order to describe the full construction of the RAID Engine we first discuss each of its inputs in greater detail.

4.1 Inputs

4.1.1 RAID code representation

In XOR-based erasure codes (RAID codes) any redundant bit is a XOR of a number of data bits. For efficiency, this relationship is applied to fix-size chunks of bits called *elements*. An element typically consists of one or more consecutive *pages* on disk. Each page is made up of multiple sectors. An element can have either data or parity pages but not a mix of the two. A *stripe* is the set of data elements and all related parity elements. A parity element in a stripe is a XOR of

Disk 1 Disk 2 Disk 3 Disk 4 Disk 5

D1	D3	D5	P1	Р3
D2	D4	D6	P2	P4

Figure 4: Physical arrangement of a stripe for a 5-disk 2-fault tolerant EVENODD code. Each strip contains 2 elements. There are 6 data and 4 parity elements in this stripe.

(D1	D2	D3	D4	D5	D6	P1	P2	Q1	Q^2
	1	0	0	0	0	0	1	0	1	0
	0	1	0	0	0	0	0	1	0	1
	0	0	1	0	0	0	1	0	0	1
	0	0	0	1	0	0	0	1	1	1
	0	0	0	0	1	0	1	0	1	1
ĺ	0	0	0	0	0	1	0	1	1	0 /

Figure 5: Generator matrix *G* for a 5-disk 2-fault tolerant EVENODD corresponding to its physical arrangement. The vertical lines mark column blocks that correspond to elements within a single strip. Here, the parity arrangement vector is $(7, 8, 9, 10)^{t}$.

some subset of data elements within that stripe. We say that the parity element depends on those data elements. The number of elements that comprise a stripe depends both on the number of disks (called *rank*) and the coding scheme. For example, the 2-fault tolerant EVENODD code over 5 devices has 10 elements in each stripe (Figure 4). Within each stripe, *e* consecutive elements are arranged contiguously on each storage device forming a *strip*. For simplicity, we assume codes that have uniform sized elements and strips.

The matrix representation of a RAID code is obtained by expressing the XOR relationships between data elements and parity elements as a system of equations [28]. The matrix from such an organization is called its *generator matrix*, *G*. It is a $N \times M$ binary matrix, where *N* is the number of data elements in a stripe and *M* is the total number of elements in a stripe (data and parity). A column of *G* corresponds to data or parity element in the stripe. A column component of *G* corresponding to a data element will usually have a single 1. For a parity element, the corresponding column component will have multiple 1's, one for each dependent data element.

If each element is k pages then, G can be rewritten in terms of pages instead of elements by replacing each element entry by an identity matrix of size k. Without loss of generality and for a simpler exposition we assume that each element corresponds to a single page and use the terms elements and pages interchangeably.

4.1.2 Layout representation

Layout is the physical (on disk) arrangement of data and parity pages within a stripe. Besides configuration parameters like the size of each page, much of the layout can be discerned from the generator matrix G for the RAID code and e, the number of pages per strip. As mentioned in the previous section, G can be visualized as blocks of e columns, each block corresponding to physical arrangement of a strip on the disk. When parity pages are interspersed with data pages the layout is interleaved. An example of an RAID code with interleaved layout is the X-Code proposed by Xu and Bruck [42] (Figure 8). Examples of codes with non-interleaved layouts include RAID 5 and EVENODD.

For convenience, it is worthwhile to summarize the location of parity pages within a stripe in a vector of column indicies corresponding to parity pages in *G*. We call this vector the parity arrangement vector of dimension $1 \times (M - N)$.

To allow for even distribution of load across all disks many layouts are cyclically shifted i.e., columns of the basic codeword are rotated distributing the parity elements evenly on all disks. This shifting can be represented by a signed number *s* that defines the cyclical shift of strips per stripe. The sign encodes the shift direction - negative for left-symmetric and positive for rightsymmetric. Some layouts have no cyclical shifting an example of which is the WEAVER family described in Hafner [19] (Figure 8).

4.1.3 Fault representation

The failure state of a page can be derived from two sources - failure state of the disks and the bad sector table. Both kinds of failure might be either discovered or obtained from system meta-data. We encode the failure state of a set of *n* pages as the fault configuration vector **f** of dimension $1 \times n$, where an entry for page *i* is marked 1 if that page has failed, otherwise 0. The fault configuration vector gets modified if new errors are discovered in while executing an I/O plan. This is shown in Figure 2.

4.1.4 Cache representation

In a write-back cache, the victim (dirty) page is determined by its replacement policy. While flushing the victim it is efficient to simultaneously flush dirty pages that belong to the same stripe [38]. In REO, we extend this idea by defining a *W*-neighborhood for a victim page. This is defined as the set of all pages, clean or dirty, in the data cache that are in a 2W + 1 stripe window centered around the victim's stripe. This is shown in Figure 6. By choosing W > 0, REO can batch flush requests of multiple pages thereby improving the throughput of the disks.



Figure 6: Figure sketches a *W*-neighborhood of a victim page chosen by the cache replacement policy based on some page list (shown at the top). All dirty pages within this 2W + 1 stripe window (centered around the victim's stripe) are written collectively at a time. Presence of clean pages within the window are leveraged to reduce I/O or XOR.

The set of pages in the *W*-neighborhood of a victim page can be partitioned into clean and dirty page sets. Each set can be encoded as a binary vector, with a 1 denoting the page in cache. We denote the two vectors - the clean data vector \mathbf{cv} and the dirty data vector \mathbf{dv} .

For write-through operations 0-neighborhood is used.

4.2 I/O plan output

As Figure 2 shows, an I/O plan is output by the RAID Engine based on the inputs we have described. Formally, an I/O plan is a 3-tuple $(\mathbf{r}, X, \mathbf{w})$. \mathbf{r} is a binary vector encoding the set of disk read operations necessary; 1 denoting that that page needs to be read. Similarly, \mathbf{w} is a binary vector encoding the set of disk write operations necessary. X is the set of XOR operations, each of which is a list of pages to be XOR-ed giving a resultant data or parity page. X can be encoded as a square matrix of dimension $M \times M$ where a column component *i* describes the set of pages to be XOR-ed to compute parity page *i*.

4.3 REO read

If the pages needed can be read from good disk(s) then, it is trivial to set \mathbf{r} to the corresponding pages on those disk(s). In this case both *X* and \mathbf{w} are zero.

The challenging case for read is when reconstruction is needed due to sector or disk failures. To derive a reconstruction strategy we employ the scheme described by Hafner et al. [7]. For completeness, we summarize their technique. Starting from the generator matrix G, a modified matrix \hat{G} is derived as follows: for every failed sector, the entries corresponding to that column in G are zeroed; for every failed disk, the columns corresponding to pages on disk are zeroed. Formally, \hat{G} is computed as follows, $\hat{G} = G(I_M - \text{diag}(\mathbf{f}))$, where I_M is the identity matrix of size M and $\text{diag}(\mathbf{f})$ is the matrix derived by applying the fault configuration vector \mathbf{f} as the diagonal of the $M \times M$ matrix.

Next, using a variant of Gaussian elimination, a pseudo-inverse $R(\hat{G}^{-1})$ is computed. R is of dimension $M \times N$ where the column component *i* corresponds to a description of the set of surviving pages (data or parity) that must be read and XOR-ed to reconstruct data page *i*.

Two aspects of this scheme, both of which are discussed and proved by Hafner et al. [7], are central to the RAID Engine's construction. The first is a result that shows that the pseudo-inverse technique will always find, if the RAID code permits, a reconstruction scheme using only the surviving pages (Theorem 1 in that reference). The second aspect is the non-uniqueness of R. From linear algebra, since \hat{G} describes an over-specified system of equations, its inverse will not be unique. Each pseudo-inverse of \hat{G} defines a read strategy. Given a resource optimization objective, an online optimizer can pick a suitable strategy and its relevant pseudo-inverse R. Column components of R that correspond to lost and required pages are extracted to **r** and X. Since some of the required pages might already be in cache, r should be logically AND-ed with the clean cache vector cv to yield the set of pages that the Execution Engine must read from disk. Note that in the case of reconstruct reads, w is zero.

4.4 **REO** write

4.4.1 Identifying affected parity pages

Recollect that the victim page to be written out is expanded to include the *W*-neighborhood of dirty pages. The dirty data vector dv is the set of pages to be written out including the victim. In any RAID code the changed content of data pages must be reflected to its dependent parity pages. Consequently, the first step is to identify all dependent parity pages. This can be determined by logically AND-ing the dirty data vector with each column component of a parity page in \hat{G} . Every resultant non-zero vector implies that the surviving parity page must be updated as part of writing dv. Parity pages with resulting zero column implies either that the parity page is unaffected or that the parity page cannot be written because of a sector or disk failure.

In this step we encode the list of affected parity pages as a binary vector where an entry for a parity page is set to 1 if that page is affected, 0 otherwise. We denote this as the affected parity vector.

4.4.2 Selecting a write strategy

The next step is to pick how each affected parity page is to be updated. In RAID 5 any parity element can be updated using one of two approaches — *parity increment* (PI) or *parity compute* (PC). With PI (a.k.a. readmodify-write), the RAID controller first reads on-disk versions of the modified data and parity pages; computes the parity difference between the new and old version of the data page and applies this increment (delta parity) to the old parity to compute the new parity. In PC, it reads all unmodified data pages from disk that a parity page depends on, XORs them with the dirty pages and computes the parity page.

The problem is how to generalize this for any RAID code under any fault configuration. To solve this, first we extend the RAID 5 approach to all RAID codes assuming fault-free configurations and then, we generalize it to allow arbitrary faults.

The extension for a write to a fault-free RAID coded volume is as follows: Any correct update of dirty pages in a RAID coded stripe is some combination of parity increment (PI) or parity compute (PC) for each of the affected parity pages. Note that updates that reuse results from one parity update (a.k.a. delta parity) for another can be re-written in a form showing as if each parity page were updated separately. Each instantiation of a PI or PC for non-zero entries in the affected parity vector defines a write strategy.

This generalization allows one to systematically enumerate all possible write strategies. For any write, if p parity pages are affected then, there will be 2^p write strategies. Since each write strategy translates to a different I/O plan, the optimizer can pick one that best matches the resource optimization objective.

To handle sector or disk failures the above extension is amended to allow reconstruction of the pages needed for PI or PC before the update of the parity page proceeds. Strategy for the necessary reconstruction(s) is chosen using the approach outlined for reo_read.

4.4.3 Deriving an I/O plan

Given a write strategy, for each affected parity page, one can compute the pages to be read, XOR-ed and written independently. REO calculates the I/O plan by combining the sub-plans for the affected parity pages. This is done by picking column components from the pseudo-inverse and translating the write strategy — PI or PC — into the necessary reads, XORs and writes. The read set is computed mindful of the clean page vector **cv**.

If the sub-plan for affected parity page k is denoted by $(\mathbf{r}_k, X_k, \mathbf{w}_k)$ then the combined I/O plan is derived by summing all the individual sub-plans.

$$\mathbf{r} = \bigvee_{k \in \text{parity}} \mathbf{r}_{\mathbf{k}}; X = \bigwedge_{k \in \text{parity}} X_k; \mathbf{w} = \bigvee_{k \in \text{parity}} \mathbf{w}_{\mathbf{k}}$$

This combined plan is submitted to the Execution Engine.

4.5 An EVENODD example

We work out an example reo_write assuming a faultfree configuration of the EVENODD code with a rank of 5 disks. The physical arrangement and generator matrix for this RAID code is shown in Figure 5. This code has two pages per strip (e = 2), 6 data pages (N = 6) and a total of 10 pages per stripe (M = 10) The parity arrangement vector is $(7, 8, 9, 10)^t$.

Let's say that there were two dirty pages - D1 and D3. Then,

$$\mathbf{d}\mathbf{v} = \begin{pmatrix} 1\\0\\1\\0\\0\\0 \end{pmatrix}$$

Say there are no clean pages ($\mathbf{cv} = \mathbf{0}$) and being fault-free ($\mathbf{f} = \mathbf{0}$), $\hat{G} = G(I_M - \mathbf{diag}(\mathbf{f})) = G$.

In the first step, the RAID Engine computes the set of affected parity pages, by AND-ing the dirty page vector with \hat{G} for each parity page. Below is a tabulation of this step for each parity page in the stripe.

P1	P2	Q1	Q2
1	0	1	0
0	0	0	0
1	0	0	1
0	0	0	0
0	0	0	0
0	0	0	0

Notice that in this write, P2 is unaffected. This is inferred by the zero column component.

Step 2 is to pick a write strategy. Say, the RAID Engine picks

strategy_A =
$$\begin{pmatrix} P1 \\ P2 \\ Q1 \\ Q2 \end{pmatrix} = \begin{pmatrix} PC \\ - \\ PC \\ PI \end{pmatrix}$$
 (1)

In Step 3 sub-plans are computed for each affected parity page. The sub-plan for P1 is

$$\mathbf{r}_{P1} = \begin{pmatrix} 0\\0\\0\\0\\1\\0\\0\\0\\0\\0\\0\\0 \end{pmatrix}; X_{P1} = \begin{pmatrix} 1\\0\\1\\0\\1\\0\\0\\0\\0\\0\\0\\0 \end{pmatrix}; \mathbf{w}_{P1} = \begin{pmatrix} 1\\0\\1\\0\\0\\0\\0\\1\\0\\0\\0\\0 \end{pmatrix}$$

The sub-plan for Q1 is

The sub-plan for Q2 is

$$\mathbf{r}_{Q2} = \begin{pmatrix} 0\\0\\1\\0\\0\\0\\0\\0\\0\\0\\1 \end{pmatrix}; X_{Q2} = \begin{pmatrix} 0\\0\\2\\0\\0\\0\\0\\0\\0\\0\\1 \end{pmatrix}; \mathbf{w}_{Q2} = \begin{pmatrix} 0\\0\\1\\0\\0\\0\\0\\0\\0\\0\\1 \end{pmatrix}$$

Note that the entry "2" denotes the XOR-ing of the old and new versions of the element.

Finally, the sub-plans are combined to give the I/O plan for this operation:

	(0)		/ P1	Q1	Q2		(1)
			1	1	0	-	$\begin{pmatrix} 1 \\ 0 \end{pmatrix}$
			0	0	0		
			1	0	2		
			0	1	0		
$\mathbf{r} =$;X =	1	1	0	; w =	
			0	1	0		
	0		0	0	0		
	0		0	0	0		0
	0		0	0	0		
	$\left(1 \right)$		0	0	1)	$\left(1 \right)$
			\ °			/	

For brevity, only the non-zero columns of X are shown above. The number atop the horizontal line denotes the column index.

For an example read operation we refer the reader to Section 7 of Hafner et al. [7].

5 Optimizer

In the previous section we discussed how the RAID Engine can enumerate all possible read or write strategies. In this section we discuss the Optimizer's online selection process. Since each strategy translates to an I/O plan, the Optimizer drives selection by defining a measure of goodness for an I/O plan.

5.1 Measures for an I/O plan

For the sake of exposition we describe two plausible measures for a I/O plan.

- The number of distinct disk read and write commands needed to execute an I/O plan. Denoted IOC, this metric is intended to measure disk overhead i.e., total seeks and rotations. In its simplest version, this measure may weight all seeks and/or rotations equally. Minimizing IOC leads to lower disk overhead in service requests which effectively improves the throughput of the disk.
- The number of cache pages input to and output from XOR operations in executing an I/O plan. Denoted XOR, this measures the memory overhead incurred. Minimizing XOR leads to lower memory bandwidth usage.

Note that alternate measures are possible. For example another metric could use variable seek and rotational costs. Yet another could use a measure of disk queue lengths. By using IOC and XOR our intent is to build a framework within which an Optimizer could be built around an objective function appropriate to the deployment scenario.

5.2 Costing an I/O plan

Given IOC and XOR as plausible metrics, the Optimizer can guide selection by costing plans from competing strategies. We describe how the Optimizer can computes these metrics from \mathbf{r} , X, and \mathbf{w} .

To compute IOC, both \mathbf{r} and \mathbf{w} are interpreted as being blocked. In the resulting vectors, a count of the number of vertical runs of non-zero entries within each block is IOC since a vertical run of non-zero entries can be submitted as one sequential I/O.

To compute XOR, simply sum up all elements in *X* and the affected parity vector.

In the example in Section 4.5, IOC = 7 and XOR = 13 for the resultant plan.

If the RAID Engine had chosen the following strategy instead of the one in Equation 1,

$$\mathbf{strategy}_B = \begin{pmatrix} P1 \\ P2 \\ Q1 \\ Q2 \end{pmatrix} n = \begin{pmatrix} PC \\ - \\ PI \\ PI \\ PI \end{pmatrix}$$
(2)

then, IOC = 8 while XOR = 12.

5.3 Selecting strategy

For a given operation, having defined the space of all possible strategies and some metric for any I/O plan, the Optimizer can employ any well-known search technique e.g., exhaustive search, dynamic programming, greedy, randomization, simulated annealing, to find the leastcost plan. The one constraint in selecting a technique is that it must be amenable to online computation. Since strategy selection is done for each I/O that requires doing disk reads and writes, some time spent selecting is acceptable. However, the time spent searching should be well worth the resulting savings in disk I/O.

5.3.1 Optimal approach

Technically, it is possible to exhaustively search for the least cost I/O plan. For reconstruct reads, each distinct pseudo-inverse leads to a strategy. For each strategy the metric for a resulting I/O plan can be computed. The number of distinct pseudo-inverses is exponential in the dimension of its null space and therefore impractical to enumerate for an implementation. A more practical heuristic is described in Hafner et. al. [7] which computes pseudo-inverses that are sparsest which potentially means least IOC or XOR.

For writes, an exhaustive enumeration of all strategies for a given operation has exponential complexity w.r.t. the total number of affected parity pages. For a given operation, the number of affected parity pages grows if a larger neighborhood is used and/or when higher fault tolerant RAID code is employed. Since exhaustive search can be CPU intensive, more practical heuristics are necessary. We describe two such heuristics - BASELINE and GRADIENT. BASELINE represents existing RAID implementations. We suggest GRADIENT as an effective heuristic among a set of search techniques (mentioned earlier) that we experimented with.

5.3.2 BASELINE heuristic

Most RAID 5 implementations (including Linux md[40]) employ a simple majority rule to determine a strategy for a write. If a majority of pages for a stripe are dirty then, PC is chosen. Else, PI is chosen. Under degraded mode, they revert to PI. Similarly, for EVEN-ODD and higher distance codes, thresholding algorithms

Algorithm 1 GRADIENT(AffectedParityVec)

- pv = sort(AffectedParityVec) {Sort affected parities in layout order.}
- 2. **strategy** = ϕ {Initialize.}
- 3. i = 0 {Iterate on each affected parity.}
- 4. while i < pv.size() do
- 5. **if** failed(**pv**[i]) **then** {Sectors for parity lost.}
- 6. i = i + 1
- 7. **continue**
- 8. end if
- 9. **strategy a strategy** {Copy strategy so far.}
- 10. $strategy_{A}[i] = PI \{ If PI \text{ for next affected parity.} \}$
- 11. $c_A = cost(strategy_A)$
- 12. **strategy**_B = **strategy** {Copy strategy so far.}
- 13. **strategy**_B[i] = PC {If PC for next affected parity.}
- 14. $c_B = cost(strategy_B)$
- 15. **if** $c_A > c_B$ **then** {PC is a better option}
- 16. strategy[i] = PC
- 17. else
- 18. strategy[i] = PI
- 19. **end if**
- 20. i = i + 1 {Move to next affected parity.}
- 21. end while
- 22. return strategy

has been suggested to determine the strategy for an entire stripe. The thresholding employed to select between PI and PC for all affected parity elements in the stripe is typically based on comparing the number of dirty pages within the stripe with a pre-computed table based on rank etc.

When dealing with failures, structure within the RAID code can be exploited to minimize recursive reconstructions [21]. The complexity of this generator is O(p) (*p* is the number of affected parity) for RAID 5 and nearly constant for thresholding schemes. In all implementations we have examined, a window size of 1 is typical i.e., a 0-neighborhood.

5.3.3 GRADIENT heuristic

The GRADIENT heuristic picks a write strategy by incrementally assigning PI or PC to each non-zero entry in the affected parity vector. As each affected parity is assigned the heuristic favors the assignment that results in a lower cost (based on IOC or XOR).

GRADIENT, outlined in the algorithm below, improves on BASELINE since a strategy for the next affected parity page is chosen based on the strategies assigned to previous parity pages. In the algorithm we have omitted obvious inputs like G, f, cv, dv, etc. The problem with GRADIENT is that, like any gradient method, there is no guarantee that it will find the optimal

plan. since it cannot avoid getting stuck in local minimas. While the complexity of this generator is comparable to BASELINE, it does requires invoking the costing routine twice for each affected parity page (lines 11 and 14). GRADIENT uses a (static) configured window size. Finding an efficient heuristic for all layouts under all workloads remains an open problem.

6 Execution engine

The Execution Engine employs well-known techniques in firmware design to execute an I/O plan. We summarize its role for clarity and completeness. As would be needed for higher throughput, multiple I/O plans will run concurrently within the Execution Engine. Each plan gets executed in three phases. In Phase 1, any reads are submitted and completed. In Phase 2, any XORs are calculated. Finally, in Phase 3, any writes are submitted and completed.

Prior to Phase 1, the Execution Engine re-blocks \mathbf{r} and \mathbf{w} just as was done in section 5.2. The resultant read and write matrices are used by the Execution Engine to coalesce multiple adjacent disk read/write requests into blocks of sequential I/Os.

6.1 Handling concurrent plans

The Execution Engine must ensure that all three phases are executed as part of a single transaction i.e., there is no interleaving of two concurrently executing IO plans that overlap. RAID controllers must reads, XORs and writes atomically to satisfy the "atomic parity update" requirement [38]. If multiple I/O plans overlap on disk sectors then, the Execution Engine must ensure that a consistent ordering of data and parity is seen by each operation. Any robust solution employs one of two techniques - on-disk log [35] or persistent memory (NVRAM). The latter approach is commonly employed in commercial RAID controllers since most do write-back caching which already requires this. In these implementations, a stripe lock table, kept in persistent memory, maintains the lock state of stripes being touched by concurrent I/O plans. The Execution Engine must acquire all locks for stripes in the W-neighborhood before beginning execution. To avoid deadlocks, all resources necessary to complete an I/O plan must be acquired in advance of the plan's execution and in a wellknow order.

6.2 Handling failures

During plan execution, various kinds of errors can occur. Errors that arise out of disk timeout or faulty XOR-ing can be easily retried by the Execution Engine. Handling errors that arise due to discovering a new media or disk failure during a plan execution requires a different tack. In this case, we suggest that the Execution Engine abort the plan and resubmit the entire operation to the RAID engine with an updated fault configuration vector. The RAID engine can compute a new (possibly better) plan that reflects the new fault state. As a side effect, the Execution Engine could update any fault meta-data managed by the system.

This step of unifying the error path with the good path in REO is possible because of the generality with which faults are handled. The elimination of potentially nested recovery paths contributes to its simplicity.

7 Other RAID operations

Besides read and write, all RAID controllers must support rebuild. Rebuild is the operation of reconstructing failed pages within a stripe and writing them to new disk locations. The rate at which rebuild is done is a primary determinant of data availability [15]. In this section we discuss how reo_rebuild can be made generic to the RAID code.

Most RAID implementations also support RAID migration, a process of re-laying data that was stored in one layout to another. Migration can include changing stripe size or its rank (5-disk RAID 5 code to 7-disk RAID 5 code) or changing the RAID code itself (5-disk 1-fault tolerant RAID 5 code to 7-disk 2-fault tolerant EVEN-ODD code). We discuss how REO can be used to support arbitrary RAID migrations.

If stripes have lost more elements from media or disk failure(s) then, the RAID code can protect against then, none of these operations can complete successfully. This is due to the inherent limitation of the RAID code and not of REO.

7.1 REO rebuild

Rebuild occurs when there is a sector or disk failure. In the former case, rebuild is typically done for the affected stripe which can be scattered over the volume. In the latter case (disk failure), rebuilds are batched. Within each batch, multiple stripes are rebuilt simultaneously since it translates to sequential disk reads and writes. Keeping a deep queue is essential to speeding up rebuilds [30]. In both cases, the basic logic for reo_rebuild remains the same.

A rebuild for a set of lost pages within a stripe is executed in two steps. In Step 1, reo_read is executed for the set of lost pages. A read strategy for reconstructing the failed pages is picked by the RAID Engine and the resultant I/O plan is executed by the Execution Engine. In Step 2, an I/O plan with \mathbf{w} set to the reconstructed pages is submitted to the execution engine. \mathbf{r} and X for such an I/O plan are zero. Note that the I/O plan in Step 2 is slightly different from one generated for a similar reo_write — in some cases, parity pages do not need to be written during rebuild. In some implementations the entire stripe is read and written out instead of just accessing the minimum pages needed for reconstruction. This is done to detect any lurking sector failures. reo_rebuild can be suitably modified to reflect this design decision. Some layouts [29] include spare space for rebuild within the stripe. Such information can be easily captured in the layout input to REO.

7.2 REO migrate

In RAID migration, a volume arranged in a source layout is re-arranged into a target layout. Typically, for space efficiency, this migration is done in-place i.e., the same set of sectors and disks in the source layout are reused for the target layout. Migration proceeds in strides, i.e., multiple stripes. Typically, this multiple is either determined by the lowest common multiple (LCM) of stride sizes of the source and target layouts, or by the stride size of the target layout alone. Sometimes, a staging area on disk is used to store temporary results if cache memory is limited. In both cases, the basic steps within reo_migrate are the same.

In a simple version, reo_migrate is executed in 2 steps. In Step 1, all data pages from the source layout are read using reo_read. Any reconstructions, if needed, are done in this step. In Step 2, the list of data pages for the target layout is input to reo_write as if all the parity pages were lost. Given this input, a good heuristic will invariably pick PC for all affected parity elements.

In an alternate implementation of reo_migrate, all pages (data and parity) in the source layout are read in Step 1. In Step 2, if possible, parity pages from this layout are reused as partial results for computing parity pages of the target page. Reusing parity pages from the source layout has the potential to reduce the memory bandwidth needed for the migration. However, it has the disadvantage that errors that have crept in due to bad sectors get propagated to the target layout.

7.3 Sundry operations

Two other operations commonly implemented are initialization and scrubbing. Initialization is layout independent in that all regions of a volume must be zero-ed. This is typically done in batches by writing sufficiently large writes with zeroes.

Scrubbing is a periodic scan of every stripe to check for latent hard errors. In REO, scrubbing is implemented by using a parity check matrix H for a RAID code which is computed from its generator matrix G. H is a $M \times (M - N)$ matrix where each column component corresponds to a parity page in the RAID code. If all pages with entry 1 in that column are XOR-ed then, the result must be a zero page. A resultant non-zero page implies an inconsistent parity. H is derived from G by

	P1	<i>P</i> 2	Q1	Q2
	1	0	1	0
	0	1	0	1
	1	0	0	1
	0	1	1	1
H =	1	0	1	1
	0	1	1	0
	1	0	0	0
	0	1	0	0
	0	0	1	0
	0 /	0	0	1 ,

Figure 7: Parity check matrix H for a 5-disk 2-fault tolerant EVENODD code (Figure 5). H is used to detect inconsistent pages. H is derived by rearranging column blocks in G into row blocks and including an identity matrix that corresponds to the parity pages.

rearranging column blocks of G into row blocks in H and including an identity matrix (corresponding to the parity pages). Figure 7 shows an example parity check matrix for the 5-disk 2-fault tolerant EVENODD code.

Rectifying stripes that fail parity check is challenging. With higher fault tolerant codes it is possible to deduce the location of the error. This is not possible with RAID 5. In some deployments silently correcting such errors is unacceptable. In cases where it is acceptable, the parity element is assumed to be wrong and fixed.

8 Evaluation

In this section we report results on aspects of REO that are amenable to quantitative evaluation. We present empirical results from our experience in adding more than a dozen RAID codes into our simulator. The efficacy of the Optimizer for real workloads is shown by trace driven simulations. Other aspects such as correctness can be shown informally leveraging results proved elsewhere [7].

8.1 Versatility

Table 1 lists a representative set of RAID codes that we implemented in a simulator. These codes vary in fault tolerance, physical arrangement, efficiency, and performance. A visual guide to stripes of these codes is shows in Figure 8. To date, we have added more than a dozen RAID codes. Adding a new code meant specifying its generator matrix and its layout, a task that averaged about 15 minutes. We believe that this empirical data can be cautiously extrapolated to real implementations while noting that it excludes the ensuing system test effort.

Fault tolerance	Code	Rank	Shift	Strip size	Stripe size (data only)	Storage efficiency
1	RAID5	8	-1	24 KB	168 KB	0.875
2	EVENODD2	7	-2	24 KB	168 KB	0.778
2	RDP	8	-2	24 KB	144 KB	0.750
2	X–Code	7	0	20 KB	140 KB	0.714
3	EVENODD3	8	-3	24 KB	168 KB	0.700
3	WEAVER3	8	-	24 KB	96 KB	0.500

Table 1: RAID codes and their layouts used in our evaluations. These layouts vary in physical arrangement, efficiency and performance. EVENODD2 and EVENODD3 are the EVENODD codes for 2 and 3 fault-tolerance respectively. WEAVER3 is the WEAVER code for 3 fault-tolerance. For fairness, we chose layout setting such that the strip size and rank remained relatively same across RAID codes.



Figure 8: A visual guide to RAID codes studied. Each square corresponds to an element on a disk. Columns of elements are physically layed contiguously on a disk. White squares represent data elements while shaded squares represent parity elements.

8.2 Efficacy of Optimizer

Although not central to the value proposition of REO, we have attempted to quantify the benefits of the Optimizer within the RAID Engine. For this we built a simulation model that included memory and I/O buses and integrated it into disksim [13], a disk simulator with fairly accurate disk and array models. We simulated the setup shown in Figure 1.

8.2.1 Setup

Table 2 lists the fixed parameters for our experiment and their values. We chose parameters corresponding to a modest RAID adapter [22].

To realistically quantify the value of the Optimizer we chose trace workloads summarized in Table 3. DS1, P5, P13 and P14 are described by Hsu [20] while TP1, TP2

Parameter	Setting
Cache size	128 MB
Page size	4 KB
Memory bus bandwidth	1 GBps
I/O bus bandwidth	500 MBps
Disk capacity	18 GB
Disk interconnect BW	150 MBps
Speed	7200 RPM
Single track seek	1.086 ms
Full seek	12.742 ms
Replacement policy	LRU
Window size (W)	0 or 2
Total write ops	100000

Table 2: Parameters used in evaluating the efficacy of Optimizer. Values were chosen to reflect a modest RAID controller. Window size was zero for BASELINE and two for GRADIENT.

and SPC1 are publicly available [39]. Given varying durations and intensities of these traces we ran our experiments for a fixed number (100,000) of write I/Os. We did two transformations on the raw traces. First we time shifted them to begin at t = 0. Second, we folded multiple LUNs in each trace into a single LUN using appropriate block offsets.

The traces in Table 3 all have a fair amount of random I/O in them. This was a deliberate choice (over picking predominantly sequential workloads) in order to make it more challenging for the Optimizer.

While running a trace, the simulator generated each I/O at the (relative) time specified in the trace. After 100,000 writes were generated, the workload was stopped and the remaining dirty pages in the cache were flushed. The run was deemed complete when there were no more dirty pages left. At the end of the run we extracted total access time from each disk in the volume. Access time for a disk request is the sum of the positioning time (includes seek, rotation, head switching, and settling times) and transfer time. The total access time is computed by summing the access times for all disk

Name	Description	LUNs	Total Size(GB)	Write(%)	Duration
DS1	SAP workload	13	46.91	90	35 mins
TP1	Transaction processing	24	26.01	60	48 mins
TP2	Transaction processing	19	8.25	17	1 hr
P5	Workstation file system workload	2	5.54	70	4 hr
P13	Workstation file system workload	3	3.24	57	26 hr
P14	Workstation file system workload	3	6.04	71	10 hr
SPC1	Storage performance council benchmark [39]	1	7.50	60	56 mins

Table 3: Traces used in this study. We show statistics for the first 100000 write I/Os of each trace that were used in our evaluations.

requests (read and write). For a given workload, total access time is a good measure of the total work done by the disks. During each run we counted the total number of bytes moved on the memory bus. We call this count the memory bus usage.

GRADIENT's objective was set to minimize IOC over XOR since disks tend to be the bottleneck. For faults we modeled static configurations where n disks in a rank were marked as failed for a n failure configuration prior to starting the trace playback. REO performed all I/O assuming such a degraded layout.

To factor out sensitivity to system settings and trace specific patterns, we normalized the total disk access time and the average memory bandwidths for GRADI-ENT to those for BASELINE. In Table 4 we show these normalized values. Total disk access time and average memory bandwidth are both lower-the-better measures. This implies that a value below 1.0 means that the optimizer using GRADIENT "outperformed" BASELINE.

For brevity, we averaged the results from each of the six application traces (excluding the synthetic benchmark SPC1) for the same layout and fault configuration. This summary from equally weighted summarization of the database and filesystem traces is labeled "Prototypical Workload" in Table 4. The results for SPC1 trace are shown in separate columns.

8.2.2 Discussion of results

Table 4 summarizes the comparison of GRADIENT to the BASELINE which approximates IBM ServeRAID adapters[22]. Since GRADIENT was setup to minimize disk I/Os, we observe that for both workloads, entries in the "Total access time" columns are less than 1.0, a measure of outperformance by GRADIENT. Of interest are the entries in the "Memory bus usage" columns. In some settings e.g., EVENODD3 with 3 faults, the savings in disk access times comes at the expense of increased memory bus usage. This occurs because the heuristic favors a strategy that minimizes IOC over XOR. An example case when this can occur is if, during a write, PI is chosen for an initial set of affected parity pages within a window. Even when it might be cheaper from a memory bandwidth standpoint to choose PC for the subsequent affected parity pages within the window, the heuristic will favor PI in order to minimize IOC. This leads to increased memory bus usage at the expense of reduced disk I/O.

Another reason why GRADIENT outperforms BASELINE on total access times for RAID 5 layouts is because of a bigger window size. Bigger window sizes improve the possibility for fewer and larger sequential I/Os.

On average, there was a modest (4—8%) reduction in disk service times using GRADIENT. The fact that the Optimizer can be competitive w.r.t. other hand tuned RAID implementations is the more important take away rather than the magnitude of its outperformance.

8.3 CPU overhead

Since we used simulations, we could not measure CPU overheads for REO overall or for GRADIENT (over BASELINE). A true measure of CPU overhead is highly sensitive to how a specific implementation is written or the compiler flags used, deployment environment, etc. Such factors are hard to extrapolate to any implementation. However, given the relative speeds of processors and disks, and the modest overhead a costing routine imposes, we believe it to be minor compared to the reduced disk service time.

9 Adaptations

In this section we discuss adaptations of REO to future trends in I/O architecture.

9.1 XOR architectures

Traditional RAID controllers have included hardware support for XOR. An XOR engine, typically built into the memory controller, allows the embedded processor to offload XOR calculations [24]. The approach for computing XOR cost metric discussed in Section 5 reflects the presence of an XOR engine. One recent trend to reduce this cost is to use commodity processors to do XOR as well as I/O handling. This allows leveraging L2 data caches in these processors by combining multiple

Code	Disk failuras	Prototypica	al workload	SPC1 w	orkload
Coue	Disk failules	Total Access	Memory bus	Total access	Memory bus
		Time	usage	time	usage
	0	0.93	0.99	0.90	1.00
KAID5	1	0.97	0.99	0.93	0.99
	0	0.97	0.99	0.93	0.90
EVENODD2	1	0.98	0.96	0.94	0.98
	2	0.99	1.08	0.92	1.17
	0	0.98	0.99	0.97	0.93
RDP	1	0.97	0.94	0.95	1.00
	2	0.98	1.04	0.93	1.25
	0	0.99	1.01	0.96	0.98
X–Code	1	0.98	0.85	0.97	0.90
	2	0.98	0.88	0.95	0.97
	0	0.97	0.91	0.92	0.82
EVENODD2	1	0.96	0.94	0.92	0.98
EVENODDS	2	0.97	1.07	0.90	1.19
	3	0.97	1.10	0.88	1.31
	0	0.97	0.99	0.96	0.98
WEAVED2	1	0.93	0.83	0.99	0.90
WEAVERS	2	0.97	0.84	1.00	0.92
	3	0.98	0.86	1.00	0.97

Table 4: Results from trace experiments. All entries in the table are normalized measures for GRADIENT w.r.t. BASELINE. An entry lower than 1.0 implies that the optimizer using GRADIENT "outperformed" BASELINE for that particular setting. Entries under "Prototypical workload" were obtained by averaging individual results for the three database and three filesystem traces. Disk failures were were assumed to be known at start of the run. Notice that, under some layouts and fault configuration, GRADIENT minimizes total access times as the expense of memory bus usage. This is consistent with its resource optimization objective of minimizing disk I/O. REO with GRADIENT is able to modestly reduce disk I/O at the expense of increased memory bus usage for common workloads.

memory fetches for a set of XOR operations with overlapping inputs into a single fetch (for each) of operands. Chunks of operand pages are fetched into the L2 cache and the resultant pages are stored into the L2 cache.

Adapting REO to this XOR architecture is simple. First, a change must be made to the algorithm that costs an IO plan for XOR. From Section 5.2, while computing the total XOR cost for an IO plan, one can count the number of non-zero entries in X in lieu of summing up all its entries. This costing change reflects the memory bandwith used when the processor calculates XOR. The second change is to the execution engine that computes XORs. If the CPU were to do the XOR operations in the I/O plan in Section 4.5 then, using the costing scheme in the previous paragraph XOR = 10.

In our experience with REO, this change of XOR calculation eliminated the memory bandwidth penalty EVENODD incurred over RDP reported by Corbett et al. [12] since common sub-expressions get automatically eliminated. Such optimizations are possible for deployments that use XOR engines at the expense of additional CPU overhead.

9.2 Hierarchical RAID architectures

Hierarchical RAID schemes are structured in layers where one RAID code is used at the top level and another at the lower level. Such layering can boost faulttolerance at the expense of storage efficiency. For sometime now, commercial RAID controllers have supported RAID 51, a hierarchical scheme which layers a RAID 5 layout over a RAID 1 layout. Of greater relevance to new RAID systems are novel intra-disk redundancy schemes like those proposed by Dholakia et. al. [10]. The goal of their scheme (called SPIDRE) is to build intra-disk redundancy aimed at reducing hard error rates in presence of correlated failures. In their analysis they show that hierarchical RAID schemes that used EVEN-ODD over disks that internally used SPIDRE had 1000x better data reliability over plain EVENODD over the same disks for common correlated sector errors.

REO can be adapted to handle such RAID scheme. To do so, one must the tensor for the product code. Working off this tensor, REO can generate I/O plans for the hierarchical RAID scheme. Any hierarchical RAID scheme will increase the number of affected parity pages for a read or write emphasizing the need for an efficient heuristic for strategy selection.

9.3 Distributed RAID architectures

Another trend in storage architectures is the rise of clustered storage systems [36, 9]. In these systems, data is striped across nodes, each of which has a network connection, processor, memory and a bunch of disks. Layouts span nodes instead of disks in traditional RAID systems. Such architectures can allow for scaling of capacity, reliability and performance at low cost [34].

Adapting to such distributed architectures requires changes to the Execution Engine. Access and updates to data striped using distributed RAID must include some serialization and recovery protocol to handle (a) transient errors from the network and/or nodes, (b) access to data from multiple clients [1], and (c) untrusted nodes [16]. Any of these proposed schemes can be implemented within the Execution Engine without changes to the RAID Engine.

10 Conclusions

We have shown REO to be an ideal solution to the problem of providing a variety of RAID codes without increasing firmware complexity. To our knowledge, REO is unique in its ability to be simultaneously flexible (supporting any XOR-based RAID code), simple (unifying fault-free and fault-ridden code paths), and self-tuning. Not only is it competitive relative to existing RAID implementations, but provides modest performance improvements for a wide range of workloads.

One possible future work would be to leverage REO for adapting data layout based on reliability, performance and efficiency attributes [41, 5].

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